

令和8年度(2026年度) 大学院工学府修士課程外国人留学生特別選抜試験 (化学工学専攻)
International Master's Programs of Chemical Engineering in the Graduate School of Engineering,
Kyushu University (Academic Year from April, 2026)

科目 / Subject : 流動 / Fluid Dynamics (1枚 / 1 sheet)

1. (20点 / 20 points)

密度 ρ , 粘度 μ をもつ流体が, 鉛直方向から角度 θ だけ傾いた平板上に形成された液膜として, 重力により定常・層流で流れ落ちている. 平板に沿った下向き方向を z , 平板に垂直な方向を x とし, 自由表面を $x = 0$, 平板表面を $x = \delta$ とする. 速度成分は流れ方向の $u_z(x)$ のみとし, 物性値は一定とする. 壁面 ($x = \delta$) では滑りなし条件が成り立つ. 以下の問いに答えよ. / A fluid of density ρ and viscosity μ flows steadily down a plane as a liquid film that is inclined at an angle θ from the vertical direction. A coordinate system is defined such that the z -axis is along the plane in the downslope direction, and the x -axis is normal to the plane. The free surface is located at $x = 0$, and the solid wall is located at $x = \delta$. The flow is two-dimensional, and the only nonzero velocity component is the downslope velocity $u_z(x)$. All physical properties are constant. At the wall the no-slip condition holds. Answer the following questions.

- (1.1) 平板に垂直な方向に微小厚さ dx の要素をとり, z 方向の運動量収支から, 液膜内の速度 $u_z(x)$ が従う支配方程式を導け. / Consider a thin shell of thickness dx in the x -direction and apply the momentum balance in the z -direction to derive the governing differential equation for $u_z(x)$.
- (1.2) 適切な境界条件を与え, 速度分布 $u_z(x)$ を求めよ. / Provide appropriate boundary conditions and determine the velocity distribution $u_z(x)$.
- (1.3) 壁面におけるせん断応力を求めよ. / Determine the shear stress on the wall surface.
- (1.4) 液膜の単位幅あたりの体積流量を求めよ. / Derive an expression for the volumetric flow rate per unit width of the film.

2. (30点 / 30 points)

内径 50.0 mm の滑らかな 100 m の円管内を, 流量が 180 L/min の水が流れている. 以下の問に答えよ. なお, 水の密度は $1.00 \times 10^3 \text{ kg/m}^3$, 動粘度は $1.00 \times 10^{-6} \text{ m}^2/\text{s}$ とする. / Water flows at a rate of 180 L/min through a smooth circular pipe with an inner diameter of 50.0 mm and a length of 100 m. Answer the following questions. The density of water is $1.00 \times 10^3 \text{ kg/m}^3$, and its kinematic viscosity is $1.00 \times 10^{-6} \text{ m}^2/\text{s}$.

- (2.1) 管内の流れにおけるレイノルズ数を求めよ. / Calculate the Reynolds number for the flow within the pipe.
- (2.2) ブラジウスの式を使って管摩擦係数を求めよ. / Calculate the friction coefficient using Blasius formula.
- (2.3) 圧力損失を求めよ. / Calculate the pressure drop.
- (2.4) 壁面におけるせん断応力を求めよ. / Calculate the shear stress on the wall surface.
- (2.5) 円管内の速度分布が $n=7$ の指数法則に従う場合の管中心の速度を求めよ. / Find the velocity at the center of the pipe when the velocity distribution within the circular pipe follows an exponential law with $n=7$.
- (2.6) 円管内の速度分布が対数法則に従う場合の管中心の速度を求めよ. / Find the velocity at the center of the pipe when the velocity distribution inside the circular pipe follows the logarithmic law.