

**International Master's Programs of Chemical Engineering in the Graduate School of Engineering,
Kyushu University (Academic Year from October, 2026)**

Subject : Basic Chemistry (1 sheet)

1. (25 points)

Answer the following questions.

Consider a particle of mass m confined in a one-dimensional infinitely deep square well potential of width L . The potential energy $V(x)$ is defined as follows:

$$V(x) = \begin{cases} 0 & (0 \leq x \leq L) \\ \infty & (x < 0, x > L) \end{cases}$$

- (1.1) Write the time-independent Schrödinger equation inside the well and find the general solution for the wave function $\Psi_n(x)$.
- (1.2) Describe the energy eigenvalues E_n .
- (1.3) Calculate the probability of finding the particle in the region $0 \leq x \leq L/4$ for the ground state ($n=1$).
- (1.4) Prove that the wave functions of $\Psi_1(x)$ and $\Psi_3(x)$ are orthogonal.

2. (15 points)

Answer the following questions.

Consider the following reaction where (*S*)-3-bromo-3-methylhexane reacts with water (H_2O) in an ethanol/water mixture. The reaction proceeds via an S_N1 mechanism. The specific rotation of (*S*)-3-bromo-3-methylhexane is $[\alpha] = +25.0^\circ$.

- (2.1) Describe the specific rotation of the product and explain the reason.
- (2.2) If the concentration of (*S*)-3-bromo-3-methylhexane is constant, and the amount of the H_2O is doubled, how will the reaction rate change? Describe the rate equation for this reaction.

3. (10 points)

Fill the blank.

Write the chemical formula and show the three-dimensional structure clearly.

